

Prototype Exercise 3

Exercises 11, 12, 13

CSC872

Pattern Analysis and Machine Intelligence

[https://bidal.sfsu.edu/~kazokada/csc872/
DATA/FaceClassification_Data.zip](https://bidal.sfsu.edu/~kazokada/csc872/DATA/FaceClassification_Data.zip)

Download it!

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Fast Prototyping Exercise

- **Fast Prototyping**
 - Learn how to do a quick proof of concept by building a prototype
 - **Correctness** matters (no sloppy algorithm!)
 - **Speed** matters (no beautification!)
 - **No perfect SE** necessary
 - **No copying of codes online.**
 - **Parameterization/Visualization/Experimentation**
 - Find out what are **free parameters** in your algorithm whose value must be hand-picked by you
 - Learn how to view internal variable's current values
 - Learn how to visualize your prototype's results in plots/images etc
 - Tweak the parameter values and study your prototype's behavior to understand the how algorithm works
- **Group Work**
 - **You are encouraged to freely exchange ideas and codes**
 - **Contributions to others are as valuable as making your own work**

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Fast Prototyping Exercise

- **Please upload your matlab codes thru iLearn forum for my grading and your playing!**
 - First two sessions: **Due on midnight of the day** (just what you did during the sessions)
 - Third last session: **Due on midnight next day** (complete version with some doc/screen shots of running the code)
- **Your grade on FP exercise will be partly based on these submitted codes and what I observe during the in-class sessions.**
- **If received helps from others and/or used codes from others, please credit the person who helped you.**

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Platforms

- **MATLAB**
 - MathWorks: <http://www.mathworks.com/>
 - <http://en.wikipedia.org/wiki/MATLAB>
- **MATLAB @ SFSU**
 - <https://at.sfsu.edu/at-mathworks-matlab>
- **Various tutorials available online**
 - https://matlabacademy.mathworks.com/?s_tid=acb_tut

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Public Libraries

- OpenCV (Computer Vision)
 - <http://www.intel.com/technology/computing/opencv/overview.htm>
- ITK (Medical Imaging)
 - <http://www.itk.org/>
- WEKA (Machine Learning)
 - <http://www.cs.waikato.ac.nz/~ml/weka/index.html>

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Classification of Facial Gender

- Learn an LDA classifier that classify input image to either female or male (binary classification)
- Smaller sized images are provided



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Paper 3

- Swets and Weng
- Using Discriminant Eigenfeatures for Image Retrieval
- PAMI, 18(8): (1996)

- A.M. Martinez, A.C. Kak,
- *PCA versus LDA*, IEEE Transactions on Pattern Analysis and Machine Intelligence, 23(2): 228-233 (2001)
- <http://www2.ece.ohio-state.edu/~aleix/>

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Data

- The same but reorganized data from the FP#1 for face recognition
- https://bidal.sfsu.edu/~kazokada/csc872/DATA/FaceClassification_Data.zip
- Images are organized in 2 folders
- Female: 54 32x32 8bit facial images
- Male: 45 32x32 8bit facial images

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Linear Discriminant Analysis

- Supervised learning for classification
- Input: Grayscale Image
 - 8bit (0-255) grayscale images of 32x32 size
- LDA projection: linear transformation to a subspace
- Threshold-based Classification: find the Bayes optimal threshold for the data after projection.
- Output: binary class labels
 - E.g., female (+1), male (-1)

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LDA Setting

- Feature extraction (projection): $\mathbf{y} = \mathbf{w}^T \mathbf{x}$
- LDA: Find \mathbf{w} such that within-class scatter (\mathbf{S}_w) is minimized and between-class scatter (\mathbf{S}_b) is maximized.
- LDA solution is given by solving a generalized eigen-value problem
 - $\mathbf{S}_b \mathbf{w} = \lambda \mathbf{S}_w \mathbf{w}$ ← *doc, eig*
 - $[V D] = \text{eig}(\mathbf{S}_b, \mathbf{S}_w)$

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LDA Limitations

- You get only $K-1$ non-zero eigen-vectors where K is the # of classes
- You need at least $K+d$ samples to have non-singular \mathbf{S}_w where d is the dimensionality of inputs
 - Singular matrix cannot be inverted!!!

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PCA+LDA Solution

- Because \mathbf{S}_w is singular you cannot solve the generalized eigenvalue problem
- Soln:
 - 1) First Perform PCA on the entire data set
 - 2) Find a subset with K top PCs that capture most of data variance
 - 3) Project all the input data points to the PCA subspace
 - 4) Compute the \mathbf{S}_w and \mathbf{S}_b with the projected datapoints in the PCA space (low-dimensional space)
 - 5) Perform LDA
 - 6) Compute the slope and intercept of the discriminant function from the LDA results

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Formulae

$$X = \{X_1, X_2, \dots, X_k, \dots, X_K\}$$

$M_k = |X_k|$: the number of samples in k -th class

$$\boldsymbol{\mu}_k = \frac{1}{M_k} \sum_{i=1}^{M_k} \mathbf{x}_i: \text{mean of } k\text{-th class}$$

$$\boldsymbol{\mu} = \frac{1}{|X|} \sum_{k=1}^K M_k \boldsymbol{\mu}_k: \text{mean of } X(\text{all})$$

$$\mathbf{S}_w = \sum_{k=1}^K \sum_{i=1}^{M_k} (\mathbf{x}_i - \boldsymbol{\mu}_k)(\mathbf{x}_i - \boldsymbol{\mu}_k)^t$$

$$\mathbf{S}_b = \sum_{k=1}^K M_k (\boldsymbol{\mu}_k - \boldsymbol{\mu})(\boldsymbol{\mu}_k - \boldsymbol{\mu})^t$$

$$\text{LDA: find } \mathbf{w} \text{ that maximizes } J(\mathbf{w}) = \frac{\mathbf{w}^t \mathbf{S}_b \mathbf{w}}{\mathbf{w}^t \mathbf{S}_w \mathbf{w}}$$

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Formulae

$$\text{LDA: find } \mathbf{w} \text{ that maximizes } J(\mathbf{w}) = \frac{\mathbf{w}^t \mathbf{S}_b \mathbf{w}}{\mathbf{w}^t \mathbf{S}_w \mathbf{w}}$$

$$\mathbf{S}_b \mathbf{w}_m = \lambda_m \mathbf{S}_w \mathbf{w}_m$$

$$\downarrow$$
$$(\mathbf{S}_w^{-1} \mathbf{S}_b) \mathbf{w}_m = \lambda_m \mathbf{w}_m$$

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Algorithm

- 1) Given labeled data $X = \{X_p, X_n\}$: female (p), male (n)
- 2) Do PCA $CV = VD$ $V = \{PC_1, \dots, PC_N\}$
 $D = \text{diag}(ev_1, \dots, ev_N)$
- 3) Find top K PCs that cover 9X% of the variance
- 4) Form PCA model F $F = \{PC_1, \dots, PC_K\}^t$
- 5) Project all data points to $FX = \{Pp, Pn\}$: $K = \# \text{ of classes}$
- 6) Compute S_w and S_b from $\{Pp, Pn\}$ $p_i = F * (x_i - \mu)$
- 7) Solve a generalized eigen-value problem with S_w and S_b
- 8) This results in a single PC: v
- 9) Compute discriminant slope $w = v' * F$
- 10) Compute discriminant intercept $b = v' * (\text{mean}Pp + \text{mean}Pn) / 2$
- 11) The result if $w * (x - \mu) - b$ is positive then (+1) otherwise (-1), (check if the sign is right)

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Useful MATLAB Codes

For LDA

- Set X as a matrix with each row is a vectorized face $\text{doc} \rightarrow \text{eig}$
- $m = \text{mean}(X)$: sampel mean of X
- $S = \text{cov}(X)$: covariance matrix (mean removed)
- Scatter matrix = $\text{cov}(X) * (N-1)$ N : # of samples in X
- $[V D] = \text{eig}(A, B)$: generalized eigenvalue problem solver
- $\text{hist}(\text{projected } X1 \text{ and } X2)$: create a histogram

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