

Fast Prototyping Exercise 1

Exercises 5, 6, 7

CSC872

Pattern Analysis and Machine Intelligence

[https://bidal.sfsu.edu/~kazokada/csc872/
DATA/FaceRecognition_Data.zip](https://bidal.sfsu.edu/~kazokada/csc872/DATA/FaceRecognition_Data.zip)

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1

1

Fast Prototyping Exercise

- **Fast Prototyping**
 - Learn how to do a quick proof of concept by building a “prototype” (from papers you read, no public codes)
 - **Correctness** matters (no sloppy algorithm!)
 - **Speed** matters (no beautification!)
 - **No perfect SE** necessary
 - **No copying of codes online (but use base Matlab functions).**
 - **When Done: Parameterization/Visualization/Experimentation**
 - Find out what are **free parameters** in your algorithm whose value must be hand-picked by you
 - Learn how to view internal variable’s current values
 - Learn how to visualize your prototype’s results in plots/images etc
 - Tweak the parameter values and study your prototype’s behavior **quantitatively** to understand the how algorithm works
- **Group Work**
 - **You are encouraged to freely exchange ideas and codes in class**
 - **Contributions to others are as valuable as making your own work**

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2

2

Fast Prototyping Exercise

- **Please upload your matlab codes thru Canvas Discussion for my grading and your playing!**
 - **Submit Codes: Fast-Prototyping: Exercise #1: Face Recognition by Eigenface/PCA**
 - **First two sessions: Due on midnight of the day** (just what you did during the sessions)
 - **Third last session: Due on midnight next day** (complete version with some doc/screen shots of running the code)
- **Your grade on FP exercises will be partly based on these submitted codes and what I observe during the in-class sessions.**
- **If received helps from others and/or used codes from others, please credit the person who helped you.**

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3

3

Platforms

- **MATLAB**
 - MathWorks: <http://www.mathworks.com/>
 - <http://en.wikipedia.org/wiki/MATLAB>
- **MATLAB @ SFSU**
 - <https://at.sfsu.edu/at-mathworks-matlab>
- **Various tutorials available online**
 - https://matlabacademy.mathworks.com/?s_tid=acb_tut

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4

4

Public Libraries

- OpenCV (Computer Vision)
 - <http://www.intel.com/technology/computing/opencv/overview.htm>
- ITK (Medical Imaging)
 - <http://www.itk.org/>
- WEKA (Machine Learning)
 - <http://www.cs.waikato.ac.nz/~ml/weka/index.html>

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5

5

Face Recognition by Eigenface

- Let's create a face recognition system using one of the most basic algorithm called "**Eigenface**".
 - You have not studied this in the lecture yet but
 - You read a paper on this (Turk & Pentland)
- You will need to implement 3 components
 - 1) **Image I/O + visualization**
 - 2) **PCA for learning/training**
 - 3) **Recognition by nearest neighbor classification**

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6

6

Paper 1

- M. Turk, A. Pentland,
- ***Eigenfaces for Recognition*, Journal of Cognitive Neuroscience, 3(1): 71-86 (1991)**
- <http://portal.acm.org/citation.cfm?id=1326887.1326894&coll=&dl=>
- <http://en.wikipedia.org/wiki/Eigenface>

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7

7

Data

- I provide a set of facial images
- https://bidal.sfsu.edu/~kazokada/csc872/DATA/FaceRecognition_Data.zip
- Images are organized in 3 folders
- **ALL** = FA+FB (for **Training**) ← PCA
- **FA**: 12 32x32 8bit facial images (for **Known faces DB**)
- **FB**: 23 facial images (for **Test Set**)

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8

8

Principal Component Analysis

- Conceptual Steps

- 1) Collect M Training Images (must be aligned, N_x by N_y matrix)
- 2) Vectorize the Images: $X = \{x_1, \dots, x_M\}$ Each of M images is a column vector with N coefficients where $N = N_x$ times N_y
- 3) Compute mean image: $\mu = \text{mean}(X)$; a vector of N coeffs
- 4) Construct Covariance Matrix: $C = (X - \mu^T)(X - \mu^T)^T$ N by N mat
- 5) Solve Eigenvalue Problem: $Cv_i = \lambda_i v_i$
- 6) Sort resulting eigen vectors in decreasing order of corresponding eigen values.
- 7) Select the top K Eigenvectors $W = \{v_1, \dots, v_K\}$, resulting in a face model $\{\mu, W\}$

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9

9

Nearest Neighbor Recognition

- Learning & Database Construction

- 1) Do PCA, yielding a face model $\{\mu, W\}$
- 2) Construct DB of known faces with codes $y_j = W^T(x_j - \mu^T)$ for all known faces $\{x_j\}$ in FA

- Face Recognition by NN Classification

- 1) Test face z is also projected to the model $W^T(z - \mu^T) = y_z$
- 2) Nearest neighbor classification of y_z with $\{y_i\}$ by picking the index “ i ” that best match to y_z according to Euclidean distance

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10

10

TRAINING	TESTING
<p>$X \leftarrow \{\text{all images in ALL}\}$</p> <p>① DO PCA on X</p> <p> \swarrow Eigen Face space. \searrow mean face $W = \begin{Bmatrix} & & \\ & \dots & \\ & & \\ \hline \text{e}_1 & & \text{e}_k \end{Bmatrix}$ $\mu = \begin{Bmatrix} \\ \\ \\ \hline \end{Bmatrix}$ </p> <p>② Choose $k = \lfloor \frac{d}{2} \rfloor$</p> <p>$\rightarrow W_k = \begin{Bmatrix} & & \\ & \dots & \\ & & \\ \hline \text{e}_1 & & \text{e}_k \end{Bmatrix}$</p>	<p>① Prepare Know Face DB. $M=12$</p> <p>For all images in FA: $\{x_1, \dots, x_M\}$</p> <p>compute $C_i = W_k^T (y_i - \mu)$</p> <p>resulting in $\{C_1, \dots, C_M\}$</p> <p>② Testing! (FR!)</p> <p>Given a test image $z \in FB$,</p> <p>compute $d_z = W_k^T (z - \mu)$</p> <p>compute distances from d_z to $\{C_i\}$</p> <p>Find index $i^* \in 1, \dots, M$ with <u>min</u> dist.</p>

Useful MATLAB Codes
<p>For PCA doc \hookrightarrow cov</p> <ul style="list-style-type: none"> • Set X as a matrix with each row is a vectorized face • $m = \text{mean}(X)$: sample mean of X, pay attention to dim. • $M = \text{repmat}(\mu', 1, N)$; create a matrix by repeating a column matrix μ' N times (M will be length of μ x N) • $S = \text{cov}(X)$: covariance matrix (mean removed) • $[V D] = \text{eig}(S)$: eigen value decomposition of a matrix S <ul style="list-style-type: none"> - Each column of V is an eigen vector. - D is a diagonal matrix of eigen values. - Columns of V and D are corresponding to each other • $d = \text{diag}(D)$; vectorize the diagonal component of a matrix • Use for-loop to get cumulative distribution of eigen values then divide it by the total variance ($\text{sum}(\text{diag}(D))$) • Plot(cumulative distribution of eigen values)